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## 1 Rigid Unit Modes in Framework Structures: Theory, Experiment and Applications

Martin T. Dove, Kostya O. Tracllenko, Matthew G. Tucker, David A. Keel)

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## Strain and Elasticity at Structural Phase Transitions in Minerals

Michael A. Carpenter

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